

## Key Concepts

Chapter 10

Snell's law

Index of refraction

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

## Takeaways

Snell's law gives the relationship between angles of incidence and refraction for a wave striking an interface between two media with different indices of refraction.

Observe that total internal reflection only occurs when the wave is passing from a medium with a higher index of refraction (lower speed) to a medium with a lower index of refraction (higher speed). This is true because the sine cannot be greater than 1.

## Things to Watch Out For

The angles in Snell's law are always measured relative to the surface normal.

## Refraction

Light is refracted as it travels from a liquid into air unless the angle of incidence is greater than or equal to  $51^\circ$ ; otherwise, no light is refracted. What is the index of refraction of the liquid?

### 1) Write Snell's law.

Use Snell's law to write an equation relating the indices of refraction in the two media to the angles in those media. The angles,  $\theta_1$  and  $\theta_2$ , are measured relative to the surface normals.

$$\begin{aligned} n_1 \sin \theta_1 &= n_2 \sin \theta_2 \\ n_{\text{liquid}} \sin \theta_1 &= n_{\text{air}} \sin \theta_2 \end{aligned}$$

### 2) Set $\theta_2 = 90^\circ$ .

When no light is refracted, total internal reflection is occurring. The critical angle is the angle at which light experiences total internal reflection. That is when  $\theta_2$  (the exit angle) is  $90^\circ$ . In this case,  $\theta_1 = \theta_{\text{critical}}$ . Solve for  $n_{\text{liquid}}$ .

$$\begin{aligned} n_{\text{liquid}} \sin \theta_1 &= n_{\text{air}} \sin \theta_2 \\ n_{\text{liquid}} \sin \theta_{\text{critical}} &= n_{\text{air}} \\ n_{\text{liquid}} &= \frac{n_{\text{air}}}{\sin \theta_{\text{critical}}} \end{aligned}$$

### 3) Plug in values.

The index of refraction of air is almost 1. Because the critical angle is less than  $90^\circ$ , the sine of the critical angle will be less than 1. Any number divided by a number less than 1 will lead to a larger result.

$$\begin{aligned} n_{\text{liquid}} &= \frac{n_{\text{air}}}{\sin \theta_{\text{critical}}} \\ n_{\text{liquid}} &= \frac{1}{\sin 51^\circ} \\ n_{\text{liquid}} &= 1.29 \end{aligned}$$

## Similar Questions

- 1) A light ray is incident on crown glass ( $n = 1.52$ ) at an angle of  $30^\circ$  to the normal. It is incident from air. What is the angle of refraction?
- 2) What is the critical angle for a diamond ( $n = 2.42$ ) to air boundary?
- 3) A light ray passes from air into an unknown substance. The incident angle is  $23^\circ$ , and the refracted angle is  $14^\circ$ . What is the index of refraction of the unknown substance?